

# 15. MAGNETIC EFFECT OF ELECTRIC CURRENT

## HOMEWORK SOLUTIONS

### 1. Given :

Effective area,

$$nA = 0.121 \text{ m}^2$$

$$\therefore nA = 1.21 \times 10^{-1} \text{ m}^2$$

$$B = 10^{-4} \text{ Wb/m}^2$$

$$i = 100 \text{ mA}$$

$$\therefore i = 10^{-1} \text{ A}$$

### To Find :

$$\tau_D = ?$$

### Formula :

$$\tau_D = niAB$$

### Solution :

Deflecting torque acting on MCG is

$$\tau_D = niAB$$

$$\therefore \tau_D = (nA)i.B$$

$$\therefore \tau_D = 1.21 \times 10^{-1} \times 10^{-1} \times 10^{-4}$$

$$\therefore \tau_D = 1.21 \times 10^{-6} \text{ Nm}$$

### 2. Given :

$$n = 1000$$

$$l = 40 \text{ mm}$$

$$\therefore l = 4 \times 10^{-2} \text{ m}$$

$$b = 30 \text{ mm}$$

$$\therefore b = 3 \times 10^{-2} \text{ m}$$

$$B = 10^{-5} \text{ Wb/m}^2$$

$$c = 10^{-7} \text{ Nm/deg}$$

$$i = 200 \text{ mA}$$

$$\therefore i = 2 \times 10^{-1} \text{ A}$$

### To Find :

$$\theta = ?$$

### Formula :

$$i = \frac{c \cdot \theta}{nAB} \quad \&$$

$$A = lb$$

### Solution :

Area of each turn of coil,

$$A = lb$$

$$\therefore A = 4 \times 10^{-2} \times 3 \times 10^{-2}$$

$$\therefore A = 12 \times 10^{-4} \text{ m}^2$$

Now,

$$i = \frac{c \cdot \theta}{nAB}$$

$$\therefore 2 \times 10^{-1} = \frac{10^{-7}}{1000 \times 12 \times 10^{-4} \times 10^{-5}} \cdot \theta$$

$$\therefore \theta = \frac{2 \times 12 \times 10^{-7}}{10^{-7}}$$

$$\therefore \theta = 24^\circ$$

### 3. Given :

Effective area,

$$nA = 10^5 \text{ mm}^2$$

$$\therefore nA = 10^5 \times 10^{-6} \text{ m}^2$$

$$\therefore nA = 10^{-1} \text{ m}^2$$

$$B = 10^{-1} \text{ Wb/m}^2$$

$$S_i = 10 \text{ degree / mA}$$

$$\therefore S_i = 10^4 \text{ degree / A}$$

### To Find :

$$c = ?$$

### Formula :

$$S_i = \frac{nAB}{c}$$

### Solution :

Current sensitivity of MCG is given by,

$$S_i = \frac{nAB}{c}$$

$$\therefore c = \frac{nAB}{S_i}$$

$$\therefore c = \frac{10^{-1} \times 10^{-1}}{10^4}$$

$$\therefore c = 10^{-6} \text{ Nm/degree}$$

**4. Given :**

Effective area,

$$nA = 10^5 \text{ mm}^2 = 10^{-1} \text{ m}^2$$

$$B = 5 \times 10^{-2} \text{ Wb/m}^2$$

$$c = 10^{-7} \text{ Nm/degree}$$

$$\theta = 10^\circ$$

**To Find :**

$$i = ?$$

**Formula :**

$$i = \frac{c}{nAB} \cdot \theta$$

**Solution :**

Current through coil of MCG is given by,

$$i = \frac{c}{nAB} \cdot \theta$$

$$\therefore i = \frac{10^{-7}}{10^{-1} \times 5 \times 10^{-2}} \times 10$$

$$\therefore i = \frac{10^{-6}}{5 \times 10^{-3}}$$

$$\therefore i = \frac{1}{5} \times 10^{-3}$$

$$\therefore i = 0.2 \text{ mA}$$

$$\therefore i = 200 \mu\text{A}$$

**5. Given :**

No. of divisions = 50

$$i_g = 100 \mu\text{A}$$

$$G = 1000 \Omega$$

**To Find :**

$$S_i = ?$$

$$S_v = ?$$

**Formula :**

$$S_i = \frac{\text{No. of divisions}}{i_g}$$

$$S_v = \frac{S_i}{G}$$

**Solution :**

$$\therefore S_i = \frac{d\theta}{di}$$

$$\therefore S_i = \frac{\text{No. of divisions}}{i_g}$$

$$\therefore S_i = \frac{50 \text{ div}}{100 \mu\text{A}}$$

$$\therefore S_i = 0.5 \text{ div}/\mu\text{A}$$

Also,

$$S_v = \frac{S_i}{G} = \frac{0.5 \text{ div}/\mu\text{A}}{1000 \Omega}$$

$$\therefore S_v = \frac{0.5}{10^3} \frac{\text{div}}{\text{mV}} = 0.5 \frac{\text{div}}{\text{mV}}$$

**6. Given :**

No. of divisions = 50

$$V_g = 25 \text{ mV}$$

$$S_i = \frac{1}{20} \frac{\text{div}}{\mu\text{A}}$$

**To Find :**

$$S_v = ?$$

$$G = ?$$

**Formula :**

$$S_v = \frac{\text{No. of division}}{V_g} \quad \&$$

$$G = \frac{S_i}{S_v}$$

**Solution :**

$$\therefore S_v = \frac{\text{No. of division}}{V_g}$$

$$\therefore S_v = \frac{50 \text{ div}}{25 \text{ mV}}$$

$$\therefore S_v = 2 \frac{\text{div}}{\text{mV}}$$

Now,

$$G = \frac{S_i}{S_v}$$

$$\therefore G = \frac{\frac{1}{20} \frac{\text{div}}{\mu\text{A}}}{2 \frac{\text{div}}{\text{mV}}}$$

$$\therefore G = \frac{1}{40} \frac{\text{mV}}{\mu\text{A}}$$

$$\therefore G = \frac{1}{40} \times \frac{10^{-3} \text{ V}}{10^{-6} \text{ A}}$$

$$\therefore G = \frac{1}{40} \times 1000 \Omega$$

$$\therefore G = 25 \Omega$$

7. Given :

$$n = 100$$

$$A = 10 \text{ cm}^2 = 10^{-3} \text{ m}^2$$

$$B = 2 \times 10^{-2} \text{ Wb/m}^2$$

$$i = 5 \times 10^{-3} \text{ A}$$

$$\theta = 60^\circ = \frac{\pi}{3}$$

To Find :

$$c = ?$$

Solution :

$$c \theta = B i n A$$

$$\therefore c = \frac{B i n A}{\theta}$$

$$c = \frac{2 \times 10^{-2} \times 5 \times 10^{-3} \times 100 \times 10^{-3}}{\pi/3}$$

$$c = \frac{3}{\pi} \times 10^{-5} \text{ Nm/rad}$$

8. Given :

$$n = 100$$

$$A = 5 \times 10^{-2} \text{ m}^2$$

$$B = 10^{-2} \text{ Wb/m}^2$$

$$c = 5 \times 10^{-9} \text{ Nm/deg}$$

To Find :

$$S_i = ?$$

Solution :

$$S_i = \frac{nAB}{c}$$

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$$= \frac{100 \times 5 \times 10^{-2} \times 10^{-2}}{5 \times 10^{-9}}$$

$$S_i = 10^7 \text{ deg/A}$$

9. Given :

$$A = 0.05 \text{ m}^2$$

$$B = 0.05 \text{ Wb/m}^2$$

$$C = 10^{-8} \text{ Nm/degree}$$

$$i = 100 \times 10^{-6} \text{ A}$$

$$n = 1$$

To Find :

$$\theta = ?$$

Formula :

$$I = \left( \frac{c}{nBA} \right) \theta$$

$$\therefore \theta = \left( \frac{nBA}{c} \right) I$$

Solution :

$$\theta = \left( \frac{1 \times 0.05 \times 0.05}{10^{-8}} \right) \times 100 \times 10^{-6}$$

$$= \left( \frac{1 \times 5 \times 10^{-2} \times 5 \times 10^{-2}}{10^{-8}} \right) \times 10^{-4}$$

$$= \frac{25 \times 10^{-4} \times 10^{-4}}{10^{-8}}$$

$$\theta = 25^\circ$$

10. Given :

$$G = 200 \Omega$$

$$i_g = 5 \text{ mA} = 5 \times 10^{-3} \text{ A}$$

$$V = 10 \text{ V}$$

To Find : Resistance R to be connected in series with MCG to convert it to measure voltages upto 10 V

Formula :

$$R = \frac{V}{i_g} - G$$

**Solution :**

$$R = \frac{V}{i_g} - G$$

$$\therefore R = \left( \frac{10}{5 \times 10^{-3}} \right) - 200$$

$$\therefore R = 1800 \, \Omega$$

**11. Given :**

$$G = 10 \, \Omega$$

$$i_g = 25 \text{ mA} = 25 \times 10^{-3} \text{ A}$$

$$V = 25 \text{ V}$$

**To Find :** Resistance R in series to convert milliammeter into voltmeter to measure upto 25 V.

**Formula :**

$$R = \frac{V}{i_g} - G$$

**Solution :**

$$R = \frac{V}{i_g} - G$$

$$\therefore R = \left( \frac{25}{25 \times 10^{-3}} \right) - 10$$

$$\therefore R = 990 \, \Omega$$

**12. Given :**

$$G = 9 \, \Omega$$

$$i_g = 1 \text{ mA} = 1 \times 10^{-3} \text{ A}$$

$$i = 1 \text{ A}$$

**To Find :** Shunt S to be connected across milliammeter to measure upto 1A.

**Formula :**

$$S = \frac{G \cdot i_g}{i - i_g}$$

**Solution :**

$$S = \frac{G \cdot i_g}{i - i_g}$$

$$\therefore S = \frac{9 \times 10^{-3}}{1 - 10^{-3}}$$

$$\therefore S = \frac{9 \times 10^{-3}}{1 - 0.001} = \frac{9 \times 10^{-3}}{0.999}$$

$$\therefore S = \frac{9}{999}$$

$$\therefore S = \frac{1}{111} \, \Omega = 0.009 \, \Omega$$

**13. Given :**

$$G \parallel S = 20 \, \Omega \text{ where}$$

$$G = 500 \, \Omega$$

**To Find :**

S & increase in current range.

**Formula :**

- i) Equivalent resistance for parallel combination. =  $G \times S / G + S$
- ii)  $\frac{i_g}{i} = \frac{S}{G + S}$

**Solution :**

$$\therefore G \parallel S = 20$$

$$\therefore 500 \parallel S = 20$$

$$\therefore \frac{500 S}{500 + S} = 20$$

$$\therefore 500 S = 10000 + 20 S$$

$$\therefore 480 S = 10000$$

$$\therefore S = \frac{10000}{480}$$

$$\therefore S = 20.83 \, \Omega$$

Also,  $S = \frac{G \cdot i_g}{i - i_g}$

$$\therefore iS - i_g S = G \cdot i_g$$

$$\therefore iS = (G + S) i_g$$

$$\therefore i = \left( \frac{G + S}{S} \right) i_g$$

$$\therefore i = \left( \frac{500 + 20.83}{20.83} \right) i_g$$

$$\therefore i = \left( \frac{520.83}{20.83} \right) i_g$$

$$\therefore i = 25 i_g$$

**14. Given :**

$$\begin{aligned} G &= 1 \Omega \\ i_g &= 100 \text{ mA} = 10^{-1} \text{ A} \\ i &= 1 \text{ A} \end{aligned}$$

**To Find :**

- i) Shunt (S) to be connected across MCG to convert it into ammeter
- ii) Effective ammeter resistance

**Formula :**

$$\begin{aligned} \text{i) } S &= \frac{G \cdot i_g}{i - i_g} \\ \text{ii) Effective ammeter resistance} \\ &= G || S \\ &= \frac{GS}{G + S} \end{aligned}$$

**Solution :**

$$\begin{aligned} \text{i) } S &= \frac{G \cdot i_g}{i - i_g} \\ \therefore S &= \frac{1 \times 10^{-1}}{1 - 0.1} = \frac{0.1}{0.9} \\ &= 0.11 \Omega \\ \text{ii) Effective ammeter resistance} &= G || S \\ &= \frac{GS}{G + S} = \frac{1 \times 0.11}{1 + 0.11} \\ &= \frac{0.11}{1.11} \\ &= 0.99 \Omega \end{aligned}$$

**15. Given :**

$$\begin{aligned} V_g &= 25 \text{ V} \text{ \&} \\ G &= 200 \Omega \\ V &= 250 \text{ V} \end{aligned}$$

**To Find :** Resistance R in series with voltmeter to increase its range upto 250 V.

**Formula :**

$$R = \frac{V}{i_g} - G \text{ where } i_g = \frac{V_g}{G}$$

**Solution :**

Full scale deflection (f-s-d) current for voltmeter is

$$i_g = \frac{V_g}{G} = \frac{25}{200} = \frac{1}{8} \text{ A}$$

Now,

$$\begin{aligned} R &= \frac{V}{i_g} - G \\ \therefore R &= \frac{250}{1/8} - 200 \\ \therefore R &= 1800 \Omega \end{aligned}$$

**16. Given :**

$$\begin{aligned} i_g &= 15 \text{ mA} \\ \therefore i_g &= 15 \times 10^{-3} \text{ A} \\ V_g &= 0.75 \text{ V} \\ \therefore V_g &= 7.5 \times 10^{-1} \text{ V} \\ V &= 150 \text{ V} \text{ \&} \\ i &= 25 \text{ A} \end{aligned}$$

**To Find :**

Shunt (S) & series resistance (R)

**Formula :**

$$\begin{aligned} S &= \frac{G i_g}{i - i_g} \text{ \&} \\ R &= \frac{V}{i_g} - G \end{aligned}$$

**Solution :**

$$\begin{aligned} S &= \frac{G i_g}{i - i_g} \\ \therefore S &= \frac{(V_g / i_g) \cdot i_g}{i - i_g} \\ \therefore S &= \frac{V_g}{i - i_g} \end{aligned}$$

$$\begin{aligned} \therefore S &= \frac{75 \times 10^{-2}}{25 - 0.015} \\ \therefore S &= \frac{75 \times 10^{-2}}{24.985} \\ \therefore S &= \frac{75}{2498.5} \\ \therefore S &= 0.03 \Omega \text{ for } 0 - 25 \text{ A range} \\ \text{Also,} \\ R &= \frac{V}{i_g} - G \\ \therefore R &= \frac{V}{i_g} - \frac{V_g}{i_g} \\ \therefore R &= \frac{150}{15 \times 10^{-3}} - \frac{75 \times 10^{-2}}{15 \times 10^{-3}} \\ &= 10^4 - 50 \\ \therefore R &= 9950 \Omega \text{ for } 0 - 150\text{V range} \end{aligned}$$

**17. Given :**

$$\begin{aligned} G &= 100 \Omega, \\ i_g &= 2 \text{ mA}, = 2 \times 10^{-3} \text{ V} \\ V &= 5 \text{ V} \\ V' &= 3\text{V} \end{aligned}$$

**To Find :**

- i) Resistance R in series with MCG to convert it into voltmeter to measure upto 5 V.
- ii) Current reading when voltmeter measure 3 V.

**Formula :**

$$\begin{aligned} \text{i) } R &= \frac{V}{i_g} - G \\ \text{ii) } i' &= \frac{V'}{R + G} \end{aligned}$$

**Solution :**

$$\begin{aligned} R &= \frac{V}{i_g} - G \\ \therefore R &= \left( \frac{5}{2 \times 10^{-3}} \right) - 100 \end{aligned}$$

$$\begin{aligned} \therefore R &= 2500 - 100 \\ \therefore R &= 2400 \Omega \\ \therefore \text{Current flowing through voltmeter when it reads 3 V is} \\ i' &= \frac{V'}{R + G} \\ \therefore i' &= \frac{3}{2400 + 100} \\ \therefore i' &= \frac{3}{2500} \\ \therefore i' &= \frac{30 \times 10^{-3}}{25} \\ \therefore i' &= 1.2 \text{ mA} \end{aligned}$$

**18. Given :**

$$\begin{aligned} i_g &= 100 \mu\text{A} \\ \therefore i_g &= 10^{-4} \text{ A}, \\ V_g &= 250\text{mV} \\ \therefore V_g &= 0.25 \text{ V} \\ i &= 10 \text{ mA} \\ \therefore i_g &= 10^{-2} \text{ A} \quad \& \\ V &= 10 \text{ V} \end{aligned}$$

**To Find :**

$$\begin{aligned} S &= ? \\ R &= ? \end{aligned}$$

**Formula :**

$$\begin{aligned} S &= \frac{Gi_g}{i - i_g} \text{ where} \\ G &= \frac{V_g}{i_g} \end{aligned}$$

**Solution :**

$$\begin{aligned} S &= \frac{V_g}{i - i_g} \\ \therefore S &= \frac{0.25}{0.01 - 0.0001} \end{aligned}$$

$$\begin{aligned} \therefore S &= \frac{0.25}{0.0099} \\ \therefore S &= 25.2 \, \Omega \text{ for 0-10 mA meter} \\ \text{Also,} \\ R &= \frac{V}{i_g} - G \\ \therefore R &= \frac{10}{10^{-4}} - \frac{0.25}{10^{-4}} \\ \therefore R &= \frac{1}{10^{-4}} (9.75) \\ \therefore R &= 97500 \, \Omega \text{ for 0 - 10 V meter} \end{aligned}$$

**19. Given :**

$$\begin{aligned} \text{No. of divisions} &= 50, \\ i_g &= 250 \, \mu\text{A}, \\ V_g &= 250 \, \text{mV} \\ i &= 0.5 \, \text{mA/div} \ \& \\ V &= 0.5 \, \text{V/div} \end{aligned}$$

**To Find :**

$$\begin{aligned} S &= ? \\ R &= ? \end{aligned}$$

**Formula :**

$$\begin{aligned} S &= \frac{G i_g}{i - i_g} \ \& \\ R &= \frac{V}{i_g} - G \end{aligned}$$

**Solution :**

$$\begin{aligned} \therefore i &= 0.5 \, \text{mA/div} \\ \therefore i &= 0.5 \times 50 \\ \therefore i &= 25 \, \text{mA} \end{aligned}$$

Also,

$$\begin{aligned} V &= 0.5 \, \text{V/div} \\ \therefore V &= 0.5 \times 50 \\ \therefore V &= 25 \, \text{V} \end{aligned}$$

Now,

$$S = \frac{G i_g}{i - i_g}$$

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$$\begin{aligned} \therefore S &= \frac{V_g}{i - i_g} \\ \therefore S &= \frac{250 \times 10^{-3}}{(25 \times 10^{-3} - 250 \times 10^{-6})} \\ S &= \frac{0.25}{0.02475} \\ \therefore S &= 10.1 \, \Omega \\ \text{Also,} \\ R &= \frac{V}{i_g} - G \\ \therefore R &= \left( \frac{25}{250 \times 10^{-6}} \right) - \frac{250 \times 10^{-3}}{250 \times 10^{-6}} \\ \therefore R &= 100000 - 1000 \\ \therefore R &= 99000 \, \Omega \end{aligned}$$

**20. Given :**

$$\begin{aligned} i_g &= 100 \, \text{mA} \\ \therefore i_g &= 10^{-1} \, \text{A}, \\ V_g &= 100 \, \text{mV} \\ \therefore V_g &= 10^{-1} \, \text{V} \\ V &= 10 \, \text{V}, \\ V' &= 7.5 \, \text{V} \end{aligned}$$

**To Find :**

- i) G
- ii) Resistance (R) in series with voltmeter to increase its range.
- iii) Current flowing through meter when it reads 7.5 V

**Formula :**

$$\begin{aligned} \text{i) } G &= \frac{V_g}{i_g} \\ \text{ii) } R &= \frac{V}{i_g} - G \\ \text{iii) } i' &= \frac{V'}{R + G} \end{aligned}$$

**Solution :**

$$\text{i) } G = \frac{V_g}{i_g}$$

$$\begin{aligned} \therefore G &= \frac{100 \text{ mV}}{100 \text{ mA}} \\ \therefore G &= 1 \Omega \\ \text{ii) } R &= \frac{V}{i_g} - G \\ \therefore R &= \frac{V}{i_g} - \frac{V_g}{i_g} \\ \therefore R &= \frac{1}{i_g} (V - V_g) \\ \therefore R &= \frac{1}{10^{-1}} (10 - 10^{-1}) \\ \therefore R &= 10(9.9) \\ \therefore R &= 99 \Omega \\ \text{iii) } i' &= \frac{V'}{R + G} \\ \therefore i' &= \frac{7.5}{99 + 1} \\ \therefore i' &= \frac{7.5}{100} \\ \therefore i' &= 75 \text{ mA} \end{aligned}$$

**21. Given :**

$$\begin{aligned} i_g &= 10 \text{ mA} \\ V_g &= 250 \text{ mV} \\ i &= 10 \text{ A} \\ V &= 100 \text{ V} \end{aligned}$$

**To Find :**

$$\begin{aligned} S &= ? \\ R &= ? \end{aligned}$$

**Solution :**

$$\begin{aligned} S &= \frac{G i_g}{i - i_g} \\ G &= \frac{V_g}{i_g} = \frac{250}{10} \\ \therefore G &= 25 \Omega \\ S &= \frac{25 (10^{-2})}{10 - 0.01} \end{aligned}$$

$$\begin{aligned} \therefore S &= \frac{25}{9.99} \times 10^{-2} \\ \therefore S &= \frac{25}{999} \Omega \\ R &= \frac{V}{i_g} - G \\ \therefore R &= \frac{100}{10^{-2}} - 25 \\ \therefore R &= 9975 \Omega \text{ in series} \end{aligned}$$

**22. Given :**

$$\begin{aligned} G &= 1000 \Omega \\ G || S &= 25 \Omega \end{aligned}$$

**To Find :**

$$S = ?$$

**Formula :**

$$G || S = \frac{GS}{G + S}$$

**Solution :**

$$\begin{aligned} \therefore G || S &= 25 \\ \frac{G \times S}{G + S} &= 25 \\ \therefore \frac{1000S}{1000 + S} &= 25 \\ \therefore 1000 S &= 25000 + 25S \\ \therefore 975 S &= 25000 \\ \therefore S &= \frac{25000}{975} \\ S &= 25.64 \Omega \end{aligned}$$

**23. Given :**

$$\begin{aligned} S_i &= 5 \text{ div/mA} \\ S_v &= 1 \text{ div/mV} \\ \text{Nof of div} &= 50 \\ i &= 5 \text{ A} \\ V &= 100 \text{ V} \end{aligned}$$

**To Find :**

$$\begin{aligned} S &= ? \\ R &= ? \end{aligned}$$



Solution :

$$\begin{aligned}
 i_g &= \frac{50}{5} = 10 \text{ mA} \\
 &= 10^{-2} \text{ A} \\
 V_g &= \frac{50}{1} = 50 \text{ mV} \\
 G &= \frac{V_g}{i_g} = \frac{50 \times 10^{-3}}{10^{-2}} \\
 &= 5 \Omega
 \end{aligned}$$

For Ammeter

$$\begin{aligned}
 S &= \frac{i_g G}{i - i_g} \\
 &= \frac{10^{-2} \times 5}{5 - 10^{-2}} \\
 &= \frac{0.05}{50 - 0.01} \\
 &= \frac{0.05}{4.99} \\
 \therefore S &= \frac{5}{499} \Omega
 \end{aligned}$$

For Voltmeter

$$\begin{aligned}
 R &= \frac{V}{i_g} - G \\
 &= \frac{100}{10^{-2}} - 5 \\
 &= 10^4 - 5 \\
 &= 10000 - 5 \\
 \therefore R &= 9995 \Omega
 \end{aligned}$$

24. Given :

$$\begin{aligned}
 S_i &= 5 \text{ div/mA} \\
 S_v &= 2 \text{ div/V} \\
 i_g &= \frac{30}{5} = 6 \text{ mA} \\
 V_g &= \frac{30}{2} = 15 \text{ V} \\
 i &= 3 \text{ A}
 \end{aligned}$$

To Find :

$$S = ?$$

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Solution :

$$\begin{aligned}
 G &= \frac{V_g}{i_g} \\
 \therefore G &= \frac{15}{6 \times 10^{-3}} \\
 \therefore G &= \frac{15000}{6} = 2500 \Omega \\
 S &= \frac{G i_g}{(i - i_g)} \\
 \therefore S &= \frac{2500 \times 6 \times 10^{-3}}{3 - 6 \times 10^{-3}} \\
 \therefore S &= \frac{15000}{3000 - 6} = \frac{15000}{2994} \\
 \therefore S &= \frac{2500}{499} \Omega
 \end{aligned}$$

25. Given :

$$\begin{aligned}
 r &= 60 \text{ cm} \\
 \therefore r &= 6 \times 10^{-1} \text{ m} \\
 B &= 0.8 \text{ T} \\
 m &= 4 \times 1.67 \times 10^{-27} \text{ kg}
 \end{aligned}$$

To Find :

$$\begin{aligned}
 \text{KE} &= ? \\
 f &= ? \\
 v &= ?
 \end{aligned}$$

Formula :

$$\text{KE} = \frac{q^2 B^2 r^2}{2m}$$

$$\text{KE} = \frac{1}{2} m v^2$$

$$v = r \omega$$

$$\omega = 2\pi f$$

Solution :

$$\text{KE} = \frac{q^2 B^2 r^2}{2m} 10^{-11}$$

$$\text{KE} = \frac{2^2 \times 1.6^2 \times 10^{-38} \times 0.8^2 \times 6^2 \times 10^{-2}}{2 \times 4 \times 1.67 \times 10^{-27}}$$

$$\begin{aligned} \text{KE} &= \frac{2.56 \times 6.4 \times 3.6 \times 10^{-3}}{8 \times 1.67} \\ \text{KE} &= \frac{1.776 \times 10^{-12}}{1.6 \times 10^{-19}} \\ \text{KE} &= \frac{1.776}{1.6} \times 10^6 \\ \therefore \text{KE} &= 11 \text{ MeV} \\ \text{KE} &= \frac{1}{2} mv^2 \\ v^2 &= \frac{2\text{KE}}{m} \\ v^2 &= \frac{2 \times 11 \times 1.6 \times 10^{-19} \times 10^6}{4 \times 1.67 \times 10^{-27}} \\ v^2 &= 5.27 \times 10^{14} \\ \therefore v &= 2.3 \times 10^7 \text{ m/s} \\ v &= r\omega \\ v &= r.2\pi f \\ f &= \frac{v}{2\pi r} \\ \therefore f &= \frac{2.3 \times 10^7}{2 \times 3.14 \times 6 \times 10^{-1}} \\ \therefore f &= 0.61 \times 10^7 \text{ Hz} \end{aligned}$$

26. Given :

$$\begin{aligned} f &= 10^7 \text{ Hz} \\ r &= 0.5 \text{ m} \\ m &= 3.34 \times 10^{-27} \text{ kg} \\ q &= 1.6 \times 10^{-19} \text{ C} \end{aligned}$$

To Find :

$$\begin{aligned} B &= ? \\ \text{KE} &= ? \end{aligned}$$

Formula :

$$\begin{aligned} \frac{mv}{r} &= qvB \\ \text{KE} &= \frac{q^2 B^2 r^2}{2m} \end{aligned}$$

Solution :

$$\frac{mv}{r} = qvB$$

$$\begin{aligned} \frac{mv}{r} &= qB \\ B &= \frac{mv}{qr} = \frac{mr.\omega}{qr} \\ B &= \frac{3.34 \times 10^{-27} \times 2\pi (10^7)}{1.6 \times 10^{-19}} \\ B &= 13.10 \times 10^{-1} \\ B &= 1.31 \text{ T} \\ \text{KE} &= \frac{q^2 B^2 r^2}{2m} \\ \text{KE} &= \frac{1.6^2 \times 10^{-38} \times 1.3 \times 1.3}{2 \times 3.34 \times 10^{-27}} \times \frac{1}{4} \\ \text{KE} &= \frac{540.8}{3.34} \times 10^{-14} \\ \text{KE} &= \frac{1.61 \times 10^{-12} \text{ J}}{1.6 \times 10^{-19}} \\ \therefore \text{KE} &= 10.10 \text{ MeV} \end{aligned}$$

27. Given :

$$\begin{aligned} r &= 0.5 \text{ m} \\ B &= 0.35 \text{ T} \\ m &= 1.67 \times 10^{-27} \text{ kg} \end{aligned}$$

To Find :

$$\text{KE} = ?$$

Formula :

$$\text{KE} = \frac{q^2 B^2 r^2}{2m}$$

Solution :

$$\begin{aligned} \text{KE} &= \frac{q^2 B^2 r^2}{2m} \\ &= \frac{1.6^2 \times 10^{-38} \times 35^2 \times 10^{-4} \times 0.25}{2 \times 1.67 \times 10^{-27}} \\ \text{KE} &= \frac{245 \times 10^{-15} \text{ V}}{1.6 \times 10^{-19}} \\ \text{KE} &= \frac{2450}{16} \times 10^{-2} \\ \text{KE} &= 1.53 \text{ MeV} \end{aligned}$$