

## PHYSICS SOLUTIONS

1. [A]

**Sol.**  $Av = A_1v_1 + A_2v_2 + A_3v_3 + A_4v_4$

$$Av = 4(A_1v_1)$$

$$12 \times 0.75 = 4 [4 \times v]$$

$$v = \frac{3}{4} \times 0.75$$

$$= 0.75 \times 0.75$$

$$v = 0.56 \text{ m/s}$$

2. [D]

**Sol.**  $Q = Av \quad v = \frac{Q}{A} = \frac{100 \times 10^{-6}}{0.25}$

$$v = 400 \times 10^{-3} \text{ mm/s} = 0.4 \text{ mm/s}$$

3. [C]

**Sol.** Let a be the size of each side of the cube. Then,

$$200 \times g = (2) \times (a^2) \times 1 \times g$$

$$\therefore a = 10 \text{ cm}$$

4. [C]

**Sol.** For equilibrium, the total upward pull will be equal to the gravitational force

$$\frac{V}{2} \times 13.6 \times g + \frac{V}{2} \times (0.8)g = V\rho g$$

$$\rho = 7.2 \text{ g/cc}$$

5. [A]

**Sol.** Velocity of efflux at a depth h is given by  $v = \sqrt{2gh}$ . Volume of water flowing out per second from both the holes are equal.

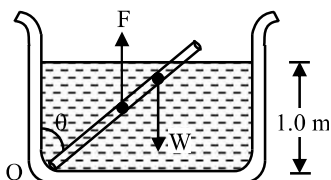
$$\therefore a_1v_1 = a_2v_2$$

$$\text{or } (L^2) \sqrt{2g(y)} = \pi R^2 \sqrt{2g(4y)}$$

$$\text{or } R = \frac{L}{\sqrt{2\pi}}$$

6. [C]

**Sol.** Length of rod inside the water =  $1.0 \sec \theta = \sec \theta$



$$\text{Upthrust } F = \left(\frac{2}{2}\right) (\sec \theta) \left(\frac{1}{500}\right) (1000) (10)$$

or  $F = 20 \sec \theta$

Weight of rod  $W = 2 \times 10 = 20 \text{ N}$

For rotational equilibrium of rod net torque about O should be zero.

$$\therefore F \left( \frac{\sec \theta}{2} \right) (\sin \theta) = W = (1.0 \sin \theta)$$

$$\text{or } \frac{20}{2} \sec^2 \theta = 20$$

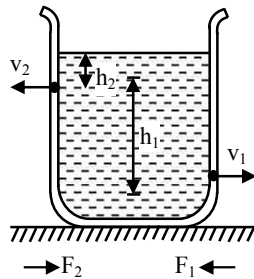
or  $\theta = 45^\circ$

$$\therefore F = 20 \sec 45^\circ$$

$$= 20\sqrt{2} \text{ N}$$

7. [C]

Sol. Thrust force



$$F = F_1 - F_2 = \rho a v_1^2 - \rho a v_2^2$$

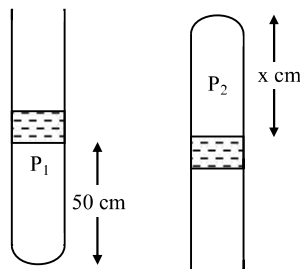
$$= \rho a (2gh_1) - \rho a (2gh_2)$$

$$= 2\rho a g (h_1 - h_2)$$

$$= 2 \rho a g h$$

8. [B]

Sol.



$$P_1 \times 50 = P_2 \times x$$

$$\Rightarrow x = \frac{50P_1}{P_2}$$

$P_1 = 80 \text{ cm of Hg}$

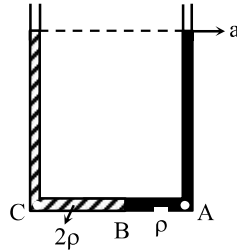
$$P_2 = 70 \text{ cm of Hg}$$

$$\therefore x = \frac{50 \times 80}{70}$$

$$= 57.12 \text{ cm} \approx 57 \text{ cm}$$

9. [B]

Sol. For the given situation, liquid of density  $2\rho$  should be behind that of  $\rho$  from right limb :



$$P_A = P_{\text{atm}} + \rho gh$$

$$P_a = P_A + \rho a \frac{\ell}{2} = P_{\text{atm}} + \rho gh + \rho a \frac{\ell}{2}$$

$$P_C = P_a + (2\rho) a \frac{\ell}{2} = P_{\text{atm}} + \rho gh + \frac{3}{2} \rho a \ell \dots(1)$$

But from left limb :

$$P_C = P_{\text{atm}} + (2\rho) gh \dots(2)$$

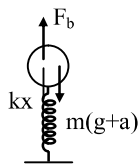
from (1) and (2)

$$P_{\text{atm}} + \rho gh + \frac{3}{2} \rho a \ell = P_{\text{atm}} + 2\rho gh$$

$$\Rightarrow h = \frac{3a}{2g} \ell$$

10. [C]

Sol.



$$\rho V(g+a) - m(g+a) = kx$$

$$(1.1)V(g+a) - 1 \times V(g+a) = 200x$$

$$x = 6 \text{ cm}$$

11. [B]

$$\text{Sol. } P_A + \frac{1}{2} \rho v_A^2 = P_B + \frac{1}{2} \rho v_B^2$$

$$P_A - P_B = \frac{1}{2} \rho (v_B^2 - v_A^2)$$

$$0.02 \times 12000 \times 10 = \frac{1}{2} \times 1000 (v_B^2 - 20.2)$$

$$4.8 = v_B^2 - 20.2 \Rightarrow v_B = 5 \text{ m/s}$$

$$\Rightarrow A_3 v_B = A_1 v_1 + A_2 v_2$$

$$\Rightarrow 30 = 4v_1 + 8$$

$$\Rightarrow 4v_1 = 22 \Rightarrow v_1 = \frac{22}{4} = 5.5 \text{ m/s}$$

12. [C]

Sol.  $h = \frac{2T \cos \theta}{\rho g} \Rightarrow r_1 h_1 = r_2 h_2$

and  $A = 2 \pi r^2 \Rightarrow r \propto \sqrt{A}$

$$\therefore \sqrt{A_1} h_1 = \sqrt{A_2} h_2$$

$$\Rightarrow \sqrt{A} \times 4 = \sqrt{\frac{A}{4}} \times h_2$$

$$\Rightarrow h_2 = 8 \text{ cm}$$

13. [A]

Sol.  $2T \ell \cos \theta = mg = \pi r^2 \ell \rho g$

$$\therefore r = \sqrt{\frac{2T}{\pi \rho g}}$$

14. [C]

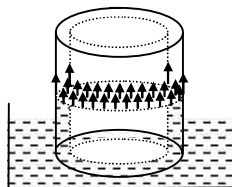
Sol. Because mercury meniscus is convex. The pressure just inside the hole will be less than the outside pressure

by  $\frac{2T}{r}$

$$\therefore h \rho g = \frac{2T}{r} \text{ or } h = \frac{2T}{r \rho g}$$

15. [D]

Sol.



Net upward force

$$= 2\pi R_2 S + 2\pi R_1 S \quad \text{contact angle} = 0^\circ$$

$\therefore$  Capillary rise is given by

$$h = \frac{2\pi S(R_1 + R_2)}{\pi(R_2^2 - R_1^2)\rho g}$$

$$= \frac{2S}{(R_2 - R_1)\rho g}$$

16. [C]

Sol.  $\frac{4}{3}\pi R^3 = n \times \frac{4}{3}\pi r^3$  or  $r = \frac{R}{n^{1/3}}$

Now work done = increase in area  $\times$  surface tension

$$= (4\pi r^2 n - 4\pi R^2) \times T = 4\pi \left( \frac{R^2}{n^{2/3}} n - R^2 \right) \times T$$

$$\propto (n^{1/3} - 1)$$

17. [B]

Sol.  $v \propto r^2$ ;  $\frac{r_1}{r_2} = \sqrt{\frac{v_1}{v_2}}$

18. [C]

Sol.  $VP^n = (V + \Delta V)(P + \Delta P)^n$

$$VP^n = VP^n \left( 1 + \frac{\Delta V}{V} \right) \left( 1 + n \frac{\Delta P}{P} \right)$$

$$\therefore \frac{\Delta V}{V} = -n \frac{\Delta P}{P}$$

$$K = - \frac{\Delta P}{\Delta V / V} = \frac{P}{n}$$

19. [A]

Sol.  $\Delta \ell = \left( \frac{\ell}{YA} \right) \cdot W$

i.e., graph is a straight line passing through origin

(as shown in question also), the slope of which is  $\frac{\ell}{YA}$ .

$$\therefore \text{Slope} = \left( \frac{\ell}{YA} \right)$$

$$\therefore Y = \left( \frac{\ell}{A} \right) \left( \frac{1}{\text{slope}} \right)$$

$$= \left( \frac{1.0}{10^{-6}} \right) \frac{(80 - 20)}{(4 - 1) \times 10^{-4}} = 2.0 \times 10^{11} \text{ N/m}^2.$$

20. [D]

Sol.  $\therefore \Delta x = \frac{F.L}{A.Y}$

$$\therefore F = \frac{Y \cdot A \cdot \Delta x}{L} \dots\dots\dots(1)$$

Volume = A.L. = A'L' = constant

$$\Rightarrow AL = 3AL'$$

$$\Rightarrow L' = L/3 \dots\dots\dots (2)$$

From equation (1)

$$\frac{F'}{F} = \frac{A'}{A} \cdot \frac{L}{L'}$$

$$= 3 \times 3$$

$$\Rightarrow F' = 9F$$

**21. [C]**

**Sol.** The density would increase by 0.1% if the volume decrease by 0.1%,

$$K = \frac{\frac{\Delta P}{\Delta V}}{V}$$

$$\Rightarrow \Delta P = K \frac{\Delta V}{V} = 2 \times 10^9 \times \frac{0.1}{100} = 2 \times 10^6 \text{ Nm}^{-2}$$

**22. [A]**

**Sol.**  $\frac{\text{Energy}}{\text{volume}} = \frac{1}{2} \times \text{stress} \times \text{strain}$

$$= \frac{1}{2} \times (Y\alpha\Delta T) \times \left(\frac{\Delta\ell}{\ell}\right) = \frac{1}{2} Y\alpha\Delta T \times \left(\frac{\ell \propto \Delta T}{\ell}\right)$$

$$= \frac{1}{2} Y \alpha^2 (\Delta T)^2 = 2880 \text{ J/m}^3$$

**23. [C]**

**Sol.**  $P = 4T/R$  ; R is less for smaller bubble, P is more for larger bubble, R is more, P is less. Since air flows from higher pressure to lower pressure therefore the air shall flow from smaller bubble to larger bubble.

**24. [B]**

**Sol.** When break into eight drop radius of small drop is  $r = \frac{R}{n^{1/3}} \Rightarrow r = \frac{R}{8^{1/3}} = \frac{R}{2}$

For large drop  $\Delta P_1 = \frac{2T}{R}$

for small drop  $\Delta P_2 = \frac{2T}{r} = \frac{2T}{(R/2)} = 2\left(\frac{2T}{R}\right)$

**25. (B)**

**26. (A)**

**Sol.** Let y be the height of liquid at some instant.

Then  $-\frac{dy}{dt} = \text{constant}$  (given)

From equation of continuity,

$$(\pi x^2) \left(-\frac{dy}{dt}\right) = a\sqrt{2gy} \quad (a = \text{area of hole})$$

Here,  $\pi\left(-\frac{dy}{dt}\right)$ ,  $a$  and  $g$  are constants

Hence, squaring the equation, we get  $y = kx^4$ .

**27. (C)**

**Sol.** From conservation of energy

$$v_2^2 = v_1^2 + 2gh \quad \dots (1)$$

[can also be found by applying Bernoulli's theorem between 1 and 2]

From continuity equation

$$A_1 v_1 = A_2 v_2$$

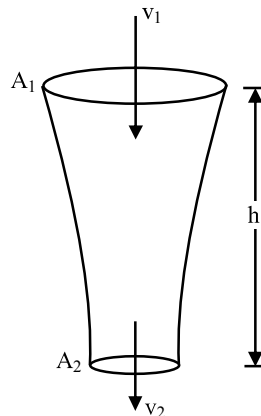
$$v_2 = \left(\frac{A_1}{A_2}\right) v_1 \quad \dots (2)$$

Substituting value of  $v_2$  from Eq. (2) in Eq. (1)

$$\frac{A_1^2}{A_2^2} \cdot v_1^2 = v_1^2 + 2gh$$

$$\text{or } A_2^2 = \frac{A_1^2 v_1^2}{v_1^2 + 2gh}$$

$$\therefore A_2 = \frac{A_1 v_1}{\sqrt{v_1^2 + 2gh}}$$



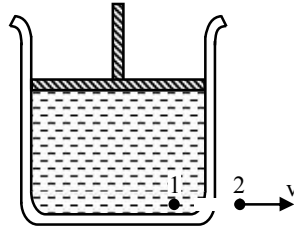
Substituting the given values

$$A_2 = \frac{(10^{-4} \text{ m}^2)(1.0 \text{ m/s})}{\sqrt{(1.0 \text{ m/s})^2 + 2(10)(0.15)}}$$

$$A_2 = 5.0 \times 10^{-5} \text{ m}^2$$

**28. (B)**

**Sol.** Applying Bernoulli's theorem at 1 and 2 : difference in pressure energy between 1 and 2 = difference in kinetic energy between 1 and 2



$$\text{or } \rho gh + \frac{mg}{A} = \frac{1}{2} \rho v^2$$

$$\text{or } v = \sqrt{2gh + \frac{2mg}{\rho A}} = \sqrt{2\left(gh + \frac{mg}{\rho A}\right)}$$

**29. (A)**

$$\text{Sol. } \Delta U = mg \left( \frac{h}{2} - \frac{h}{6} \right) = mg \frac{h}{3}$$

$$= Adhg \cdot \frac{h}{3} = \frac{Adh^2g}{3}$$

**30. (A)**

**Sol.** Fraction of volume immersed is independent of effective  $g$