

PHYSICS - SOLUTION

1. d) In a sonometer,

$$v \propto \sqrt{T} \therefore \frac{v_1}{v_2} = 2 = \sqrt{\frac{T_1}{T_2}} \Rightarrow T_2 = \frac{T_1}{4}$$

$$\therefore \text{ \%change will be: } \frac{T_1 - T_2}{T_1} \times 100 = \frac{T_1 - \frac{T_1}{4}}{T_1} \times 100 = 75\%$$

2. d) For waves along a string :

$$v \propto \sqrt{T} \Rightarrow \lambda \propto \sqrt{T}$$

$$\text{Now, for 6 loops : } 3\lambda_1 = L \Rightarrow \lambda_1 = L/3$$

$$\& \text{ for 4 loops : } 2\lambda_1 = L \Rightarrow \lambda_2 = L/2$$

$$\Rightarrow \frac{\lambda_1}{\lambda_2} = \frac{2}{3} \Rightarrow T_2 = \frac{9}{4} \times T_1 = \frac{9}{4} \times 36 = 81 \text{ N.}$$

3. c) Velocity of sound is inversely proportional to the square root of density of the medium.

$$\text{i.e., } V\sqrt{\rho} = \text{constant} \Rightarrow \frac{V_1}{V_2} = \sqrt{\frac{\rho_2}{\rho_1}} = \sqrt{\frac{2\rho}{\rho}} = \sqrt{2}$$

$$4. \text{ c) } y = \log \frac{x^2 - t^2}{x - t} = \log(x + t) \quad \left(\because \log a - \log b = \log \frac{a}{b} \right)$$

$$\frac{\partial y}{\partial x} = \frac{1}{(x+t)}$$

$$\frac{\partial^2 y}{\partial x^2} = \frac{1}{(x+t)^2}$$

and

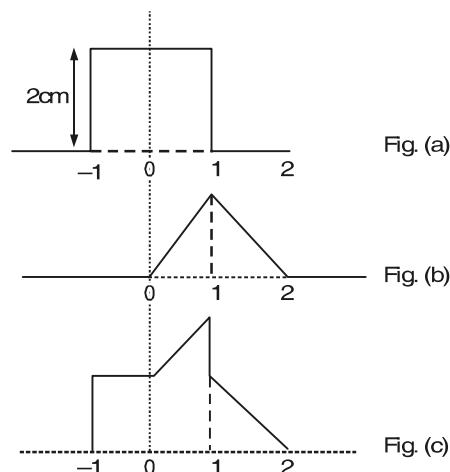
$$\frac{\partial y}{\partial t} = \frac{(\partial x / \partial t)}{(x+t)} = \frac{v}{(x+t)}$$

$$\frac{\partial^2 y}{\partial t^2} = -\frac{v^2}{(x+t)^2}$$

$$\Rightarrow \frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}$$

Which is the general form of wave equation.

5. d) At $t = 2$ second, the position of both pulses are separately given by fig. (a) and fig. (b); the superposition of both pulses is given by fig. (c)



6. b) $dm \cdot \omega^2 R = 2T \sin \frac{d\theta}{2}$

$$\mu R d\theta \omega^2 R = 2T \frac{d\theta}{2}$$

$$\Rightarrow \mu \omega^2 R^2 = T \quad \Rightarrow v_w = \sqrt{\frac{T}{\mu}} = \sqrt{\omega^2 R^2} = \omega R$$

Also speed of string is ωR

\therefore The velocity of disturbance w.r.t. ground = $\omega R + \omega R = 2\omega R$.

7. c) Let ℓ be the length of rope. Then tension in the string at height h will be:

$$T = \frac{m}{\ell} hg \quad u = \sqrt{\frac{T}{\mu}}$$

Here, $\mu = \text{mass per unit length} = \frac{m}{\ell}$

$$\therefore u = \sqrt{gh} \text{ or } u^2 = gh$$

i.e., u versus h graph is a parabola.

8. b) Let a_i and a_r be the amplitudes of incident and reflected wave. Then

$$\frac{a_i + a_r}{a_i - a_r} = n \text{ (Given)}$$

$$\therefore \frac{a_r}{a_i} = \left(\frac{n-1}{n+1} \right)$$

\therefore Fraction of energy reflected is

$$\frac{E_r}{E_i} = \left(\frac{a_r}{a_i} \right)^2 = \left(\frac{n-1}{n+1} \right)^2$$

9. a) $f_0 = \frac{v}{2\ell}$

Now beat frequency = $f_1 - f_2$

$$= \frac{v}{2\left(\frac{\ell}{2} - \Delta\ell\right)} - \frac{v}{2\left(\frac{\ell}{2} + \Delta\ell\right)} = \frac{v}{2} \left[\frac{1}{\frac{\ell}{2} - \Delta\ell} - \frac{1}{\frac{\ell}{2} + \Delta\ell} \right]$$

$$= (f_0 \ell) \left[\frac{2}{\ell - 2\Delta\ell} - \frac{2}{\ell + 2\Delta\ell} \right] = (f_0 \ell) \left[\frac{1 + 2\Delta\ell - \ell + 2\Delta\ell}{\ell^2 - 4(\Delta\ell)^2} \right] \approx 2f_0 \ell \left(\frac{4\Delta\ell}{\ell^2} \right) \approx \frac{8f_0 \Delta\ell}{\ell}$$

10. c) $v = \sqrt{T/\mu}$ or $v \propto \frac{1}{\mu} \rightarrow 1 \rightarrow RP, 2 \rightarrow PQ, 3 \rightarrow QS$

Here μ is mass per unit length.

$$\mu_1 = \frac{0.1}{2} = 0.05 \text{ kg/m}$$

$$\mu_2 = \frac{0.1}{3} = 0.067 \text{ kg/m} \quad \text{and} \quad \mu_3 = \frac{0.15}{4} = 0.0375 \text{ kg/m}$$

$$\mu_3 < \mu_1 < \mu_2$$

Between string RP and PQ, medium of string PQ is denser. Therefore, wave-2 will suffer a phase change of π . Between string PQ and QS, medium of string PQ is denser. Therefore wave 4 will not suffer any phase change.

11. c) This problem is a Doppler effect analogys
where $f = 20/\text{min}$, $v = 300 \text{ m/min}$
and $v_s = 30 \text{ m/min}$

$$\square \quad f_{\text{d}} = f \left(\frac{v}{v - v_s} \right) = (20) \left(\frac{300}{300 - 30} \right) = 22.22 \text{ min}^{-1}$$

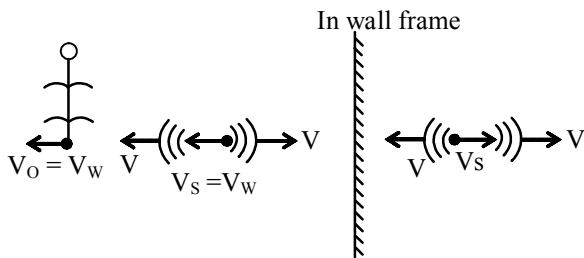
12. c) The wavelength of sound source = $\frac{330}{110} = 3 \text{ metre}$.

The phase difference between interfering waves at P is

$$= \times \square = \frac{2\pi}{\lambda} (S_2P - S_1P) = \frac{2\pi}{3} (5 - 4) = \frac{2\pi}{3}$$

$$\square \text{ Resultant intensity at P} = I_0 + 4I_0 + 2\sqrt{I_0} \sqrt{4I_0} \cos \frac{2\pi}{3} = 3 I_0$$

13. D) 330 Hz



$$f_{\text{echo}} = f_{\text{ac}} \left[\frac{V - V_0}{V + V_s} \right] = 334 \left[\frac{330 - 2}{330 + 2} \right]$$

$$= 334 \times \frac{328}{332} = 330 \text{ Hz}$$


14. b)


$$\text{Fundamental frequency of wire } (f_{\text{wire}}) = \frac{v}{2\ell}$$

a)

$$f = \frac{v}{4\ell}, \frac{3v}{4\ell}, \frac{5v}{4\ell} \text{ cannot match with } f_{\text{wire}}$$

b) $f = \frac{v}{2(2\ell)}, \frac{v}{2(2\ell)}, \frac{3v}{2(2\ell)}$ its second harmonic $\frac{2v}{2(2\ell)}$ matches with f_{wire} .

c)  $f = \frac{v}{2(\ell/2)}, \frac{2v}{2(\ell/2)}$ cannot match with f_{wire}

d)  $f = \frac{v}{4(\ell/2)}, \frac{3v}{4(\ell/2)}$... cannot match with f_{wire}

15. b) $V_s = 4 \text{ km/sec}$ $v_p = \sqrt{\frac{y}{\rho}} = \sqrt{\frac{12.8 \times 10^{10}}{2000}} = 8000 \text{ m/sec} = 8 \text{ km/sec}$

$$\frac{\ell}{v_s} - \frac{\ell}{v_p} = 3 \text{ min} = 3 \times 60 \text{ sec.}$$

$$\frac{\ell}{4} - \frac{\ell}{8} = 3 \times 60 \quad \ell = 1440 \text{ km}$$

16. b) Towards right wavelength gets compressed, towards left, wavelength gets expanded.

17. d) x_1 and x_2 are in successive loops of std. waves.

so $\phi_1 = \frac{2\pi}{\lambda}$

and $\phi_2 = K(\Delta x) = K\left(\frac{3\pi}{2K} - \frac{\pi}{3K}\right) = \frac{7\pi}{6} = \frac{\phi_1}{6} = \frac{6}{7}$

18. b) $V_s = \sqrt{\frac{Y}{\rho}} = \sqrt{\frac{10^{11}}{10.0 \times 10^4}} = 10^3 \text{ m/sec.}$

$$t = \frac{2\ell}{V} = \frac{2 \times 100}{1000} = 0.2 \text{ sec}$$

19. c) $V_{\text{max}} = \omega_n A$
 $= (24^{1/2} f) A$
 $= (24^{1/2}) (440) (10^{-6})$
 $= 2.76 \times 10^{-3} \text{ m/sec.}$

20. c) Apparent frequency

$$n_d^a = n \frac{(u + v_w)}{(u + v_w - v_s \cos 60^\circ)} = \frac{510(330 + 20)}{330 + 20 - 20 \cos 60^\circ} = 510 \times \frac{350}{340} = 525 \text{ Hz}$$

21. a) For minimum,

$$\Delta x = (2n - 1) \frac{\lambda}{2}$$

The maximum possible path difference = distance between the sources = 3m.

For no minimum

$$\frac{\lambda}{2} > 3$$

$$\frac{2}{\lambda} > 6 \quad \therefore f = \frac{V}{\lambda} < \frac{330}{6} = 55$$

\therefore If $f < 55 \text{ Hz}$, no minimum will occur.

22. a) The speed of sound in air is $v = \sqrt{\frac{\gamma RT}{M}}$

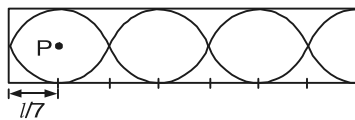
$\frac{\gamma}{M}$ of H_2 is highest, hence speed of sound in H_2 shall be maximum.

23. b) As $y = A_b \sin(2\pi n_{av}t)$
 where $A_b = 2A \cos(2\pi n_2 t)$

where $n_A = \frac{n_1 - n_2}{2}$

24. a) The figure shows variation of displacement of particles in a closed organ pipe for 3rd overtone.

For third overtone $\ell = \frac{7\lambda}{4}$ or $\frac{4\ell}{7} = \frac{\lambda}{4} = \frac{\ell}{7}$



Hence, the amplitude at P at a distance $\frac{\ell}{7}$ from closed end is 'a' because there is an antinode at that point.

Alternate: a)

Because there is node at $x = 0$ the displacement amplitude as function of x can be written as

$$A = a \sin kx = a \sin \frac{2\pi}{\lambda} x$$

For third overtone $\ell = \frac{7\lambda}{4}$ or $\frac{4\ell}{7} = \frac{\lambda}{4}$

$\therefore A = a \sin \frac{7\pi}{2} \frac{\ell}{7} = a \sin \frac{\pi}{2} = a$ at $x = \frac{\ell}{7}$ \square $A = a$

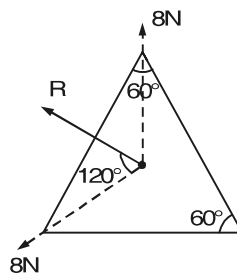
25. d) For a stationary observer between wall and source,

frequency, from direct source = $\left(\frac{V}{V - V_s}\right) f_0$

frequency, from reflected sound = $\left(\frac{V}{V - V_s}\right) f_0$

So no beats will be heard.

26. d) $R = \sqrt{8^2 + 8^2 + 2 \cdot 8 \cdot 8 \cos 120^\circ} = 8 \text{ N}$



27. b) Speed will be maximum when acceleration becomes zero.

i.e., when $kx = EQ$ \square $X = \frac{EQ}{K}$

By work-energy theorem: $W_{\text{all}} = \times KE$ \square $EQX - \frac{1}{2}KX^2 = 0$; $X_{\text{max}} = \frac{2EQ}{K}$

28. c) The acceleration of centre of mass of system of particles is

$$a_{\text{cm}} = \frac{(q_1 + q_2) E}{2m}$$

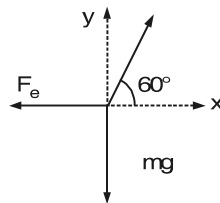
\square x-coordinate of centre of mass at $t = 2$ second is

$$X_{\text{cm}} = \frac{1}{2} a_{\text{cm}} t^2 = \frac{1}{2} \frac{q_1 + q_2}{2m} E \times 2^2 = \frac{q_1 + q_2}{m} E$$

Let the x-coordinates of q_1 and q_2 at $t = 2$ sec be x_1 and x_2 [$x_1 = 2a$ at $t = 2$ sec.]

$$\square X_{\text{cm}} = \frac{mx_1 + mx_2}{2m} = \frac{x_1 + x_2}{2} \text{ or } x_2 = 2 X_{\text{cm}} - x_1 = 2 \frac{(q_1 + q_2) E}{m} - 2a .$$

29. a) The bowl, exerts a normal force N on each bead, directed along the radius line or at 60° above the horizontal. Consider the free-body diagram of the bead on the left with the electric force F_e applied.



$$\square F_y = N \sin 60^\circ - mg = 0, \quad \square N = mg / \sin 60^\circ$$

$$\square F_x = -F_e + N \cos 60^\circ = 0, \quad \square \frac{Kq^2}{R^2} = N \cos 60^\circ = \frac{mg}{\tan 60^\circ} = \frac{mg}{\sqrt{3}}$$

$$k = \frac{1}{4 \pi \epsilon_0}$$

Thus $q = R \left(\frac{mg}{k\sqrt{3}} \right)^{1/2}$

30. a) We have centripetal force equation

$$q \left(\frac{2k\lambda}{r} \right) = \frac{mv^2}{r}$$

so $v = \sqrt{\frac{2kq\lambda}{m}}$ Now, $T = \frac{2\pi r}{v} = \sqrt{\frac{m}{2k\lambda q}}$

where, $k = \frac{1}{4\pi\epsilon_0}$