

PHYSICS PAPER I

MORE THAN ONE CORRECT TYPE

Q. 1

Sol. [a, b]

If $q_1 = q_2 = Q$

$$F_i \propto q_1 q_2 \quad \therefore F_i \propto Q^2$$

After touching new charges on each

$$\text{ball is } \frac{Q_1 + Q_2}{2} = \frac{2Q}{2} = Q$$

$$F_{\text{new}} \propto Q^2$$

$$\therefore F_i = F_{\text{new}}$$

if $q_1 \neq q_2$

$$F_{\text{new}} = \left(\frac{q_1 + q_2}{2} \right)^2$$

$$= \frac{q_1^2}{4} + \frac{q_2^2}{4} + \frac{2q_1 q_2}{4}$$

$$F_{\text{new}} > F_i$$

Q.2 [a,b,c,d]

Sol.

$$a = \frac{F}{m} = \frac{qE}{m} = \frac{q(\alpha - \beta x)}{m}$$

$$a = 0 \text{ at } x = \frac{\alpha}{\beta}$$

Force on the particle is zero at $x = \frac{\alpha}{\beta}$

So, mean position of particle is at $x = \frac{\alpha}{\beta}$

$$\frac{v dv}{dx} = \frac{q}{m} (\alpha - \beta x)$$

$$\text{Solve for } v = \sqrt{\frac{2qx}{m} \left(\alpha - \frac{\beta}{2} x \right)}$$

$$v = 0 \text{ at } x = 0 \text{ and } x = \frac{2\alpha}{\beta}$$

So the particle will oscillate between $x = 0$ to $x = \frac{2\alpha}{\beta}$ with mean position at $x = \frac{\alpha}{\beta}$. Therefore

amplitude of particle is $\frac{\alpha}{\beta}$.

Maximum acceleration of particle is at extreme position (at $x = 0$ or $x = \frac{2\alpha}{\beta}$) and $a_{\max} = \frac{q\alpha}{m}$.

Q.3 [a,c,d]

Sol. The potential at surface, 5 cm from surface and 10 cm from surface outwards is

$$V_s = \frac{KQ}{R} \quad \dots\dots(1)$$

$$\frac{KQ}{R+5} = 100 \quad \dots\dots(2)$$

$$\frac{KQ}{R+10} = 75 \quad \dots\dots(3)$$

From equation (2) and (3) $\Rightarrow R = 10$ cm

\therefore from equation (2)

$$Q = \frac{100 \times 15 \times 10^{-2}}{9 \times 10^9} = \frac{5}{3} \times 10^{-9} \text{ C}$$

\Rightarrow B is false

$$V_{\text{surface}} = \frac{KQ}{R} = \frac{100 \times (R+5)}{R} = \frac{100 \times 15}{10} = 150 \text{ V} \Rightarrow \text{A is true}$$

$$V_{\text{centre}} = \frac{3}{2} \frac{KQ}{R} = 225 \text{ volts}$$

\Rightarrow D is true

$$E_{\text{surface}} = \frac{KQ}{R^2} = \frac{150}{10 \times 10^{-2}} = 1500 \text{V/m}$$

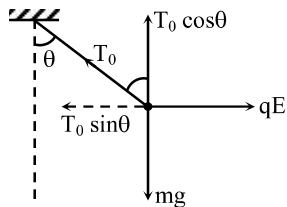
⇒ C is true

Q.4 bcd

SOLN. Potential at each point on y-z plane is zero. The electric field will be zero on y-z plane at a distance $\sqrt{2}a$ from origin.

Q.5

Sol. [a,d]



$$E = \sigma/2\epsilon_0$$

$$T_0 \cos\theta = mg$$

$$T_0 \sin\theta = qE$$

$$\tan\theta = \frac{q}{mg} \quad (\sigma/2\epsilon_0)$$

$$\text{As } T_0 = \sqrt{(mg)^2 + (qE)^2}$$

$$\text{i.e. } T_0 > mg$$

i.e. the effective value of g is increased, hence time period of oscillation decreases.

Q.6 [a,c]

Sol. At the instant shown, both particles are at their mean position and moving in opposite directions. Phase difference = 180°

As ' ω ' is same for both particles

$\left\{ \omega = \sqrt{\frac{GM}{R^3}} \right\}$ the phase difference will be maintained throughout and they can never meet.

$v_{\text{max}} = A\omega \rightarrow$ For particle undergoing S.H.M.

$$\therefore \frac{v_1}{v_2} = \frac{R}{R/2} = \frac{2}{1}$$

Q.7 [a,b,c]

Sol.

$$v^2 = 144 - 9x^2$$

$$2v \frac{dv}{dx} = -18x$$

$$\therefore v \frac{dv}{dx} = -9x \Rightarrow \omega = 3 \Rightarrow T = \frac{2\pi}{3} \text{ units}$$

$$\text{Also, } v^2 = 144 - 9A^2 = 0$$

$$A = 4 \text{ units}$$

$$\text{Now, } |a| = \omega^2 x = 9 \times 3 = 27 \text{ units}$$

Q.8 [a,d]

Sol.



Let velocity of vehicle be v_0

$$\therefore n_1 = \frac{v + v_0}{v - v_0} \cdot v$$

$$\Rightarrow n_1 = \frac{2v_0 v}{v - v_0} \quad \dots(i)$$

$$n_2 = v - \frac{v - v_0}{v + v_0} \cdot v$$

$$\Rightarrow n_2 = \frac{2v v_0}{v + v_0} \quad \dots(ii)$$

[Where v = Frequency of horn

v = Velocity of sound in air]

From (i) and (ii)

$$v = \frac{n_1 n_2}{n_1 - n_2}$$

$$\text{and } v_0 = \frac{n_1 - n_2}{n_1 + n_2} \cdot v$$

Q.9 [b, c]

Sol. As $f_1 : f_2 : f_3 = 3 : 5 : 7$,

string is fixed at one end. Its fundamental frequency is $f_0 = \frac{f_1}{3} = \frac{105}{3} = 35$ Hz.

Q.10. abcd

Conceptual

MATRIX MATCH TYPE

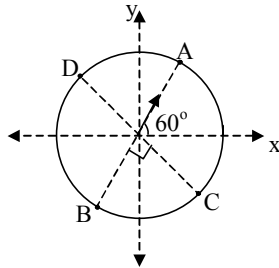
1. A – S B – PQR C – QR D – S

Conceptual

2. A – P B – RS C – PQ D – RS

The resultant dipole moment has magnitude $\sqrt{(\sqrt{3}P)^2 + P^2} = 2P$ at an angle

$$\theta = \tan^{-1}\left(\frac{\sqrt{3}P}{P}\right) = 60^\circ \text{ with the positive x-direction.}$$



Diameter AB is along net dipole moment and diameter CD is normal to net dipole moment.

Potential at A $\left(\frac{R}{2}, \frac{\sqrt{3}R}{2}\right)$ is maximum.

Potential is zero at C $\left(\frac{\sqrt{3}R}{2}, -\frac{R}{2}\right)$ and D $\left(-\frac{\sqrt{3}R}{2}, \frac{R}{2}\right)$.

Magnitude of electric field is $\frac{1}{4\pi\epsilon_0} \frac{4p}{R^3}$

At A $\left(\frac{R}{2}, \frac{\sqrt{3}R}{2}\right)$ and B $\left(-\frac{R}{2}, -\frac{\sqrt{3}R}{2}\right)$

Magnitude of electric field is $\frac{1}{4\pi\epsilon_0} \frac{2p}{R^3}$ at C $\left(\frac{\sqrt{3}R}{2}, -\frac{R}{2}\right)$ and D $\left(-\frac{\sqrt{3}R}{2}, \frac{R}{2}\right)$.

INTEGER TYPE

1. 0

2.

$$\tan \theta = \frac{F}{mg} \quad \tan \theta^1 = \frac{F}{kmg \left(1 - \frac{\sigma}{\rho}\right)}$$

$$\frac{F}{mg} = \frac{F}{kmg \left(1 - \frac{\sigma}{\rho}\right)}$$

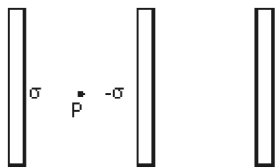
As $\theta^1 = \theta$ we have

$$\Rightarrow k = 2$$

3. 8

4. 2

5.



From Gauss theorem surface charge density on C face is $-\sigma$.

$$\therefore E_p = \frac{\sigma}{2\epsilon_0} + \frac{\sigma}{2\epsilon_0} = \frac{\sigma}{\epsilon_0} = 5.0 \text{ N/C}$$

6. 9

Potential due to a dipole $V = \frac{Kp}{r^2} = \frac{K(\vec{p} \cdot \vec{r})}{r^3}$

Then $\vec{r} = \vec{r}_N - \vec{r}_M = (4\hat{i} - \hat{j}) - (2\hat{i} - 3\hat{j} + \hat{k})$

$$\vec{r} = 2\hat{i} + 2\hat{j} - \hat{k}$$

$$\therefore |\vec{r}| = \sqrt{2^2 + 2^2 + (-1)^2} = 3$$

$$\therefore V = \frac{9 \times 10^9 \times (9\hat{i} + 3\hat{j} - 3\hat{k}) \cdot (2\hat{i} + 2\hat{j} - \hat{k})}{3^3} = \frac{9}{27} \times 10^9 \times [18 + 6 + 3] = 9 \times 10^9$$

7.

Sol. [5]

$$AP = 4.47 \text{ m}$$

$$BP = 4.12 \text{ m}$$

$$d = 0.35 \text{ m}$$

destructive

$$d = \frac{\lambda}{2}$$

$$\lambda = 2d$$

$$f = \frac{v}{\lambda} = 500 \text{ Hz.}$$

$$= 5 \times 10^2 \text{ Hz}$$

$$\therefore n = 5$$

8.

Sol. [2]

$$f_1 = \frac{300+30}{300} .f$$

$$f_2 = \frac{300-30}{300} .f$$

$$v = f_1 - f_2 = 2 \text{ Hz}$$